Hypersurfaces of two space forms and conformally flat hypersurfaces

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Abstract. In this talk, we discuss the problem of determining the hypersurfaces $f: M^n \to \mathbb{Q}_s^{n+1}(c)$ with dimension $n \ge 3$ of a pseudo-Riemannian space form of dimension n+1, constant curvature c and index $s \in \{0, 1\}$ for which there exists another isometric immersion $\tilde{f}: M^n \to \mathbb{Q}_t^{n+1}(\tilde{c})$ with $c \ne c$. For $n \ge 4$, we extend results for s = 0 = t by do Carmo and Dajczer and by Dajczer and the second author, thus providing a complete solution in that case. Our main result is a characterization of the solutions that have dimension n = 3 and three distinct principal curvatures. We obtain a similar characterization of conformally flat hypersurfaces of $\mathbb{Q}_s^4(c)$ with three distinct principal curvatures, which improves a theorem by Hertrich-Jeromin. We also derive a Ribaucour transformation for both classes of hypersurfaces, which enables to produce new elements of those classes, starting from a given one, in terms of solutions of a linear system of PDE's. The talk is based on joint work (in preparation) with S. Canevari.